

Episode 6.04 - Four-Variable Karnaugh Map Example

(Transcript URL: <https://intertainment.com/episode-6-04-four-variable-karnaugh-map-example/>)

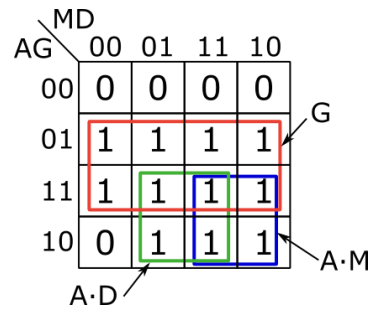
Show Description: Many digital designs begin with a truth table. In this episode, we do just that, and then create the simplified sum-of-products expression by way of the Karnaugh map.

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0:55	<p>Example truth table for a security system. Inputs identifiers are:</p> <ul style="list-style-type: none"> • A = 1, system is armed; A = 0, system is disarmed • G = 1, glass break has been detected; G = 0, no glass break detected • M = 1, motion has been detected; M = 0, no motion detected • D = 1, door is open; D = 0, door is closed • X = 1, alarm is sounding; X = 0, alarm is silent <table style="margin-left: 40px; border-collapse: collapse;"> <thead> <tr> <th style="border-right: 1px solid black; padding: 5px;">A</th> <th style="padding: 5px;">G</th> <th style="padding: 5px;">M</th> <th style="border-right: 1px solid black; padding: 5px;">D</th> <th style="padding: 5px;">X</th> <th style="padding: 5px;"></th> </tr> </thead> <tbody> <tr> <td style="border-right: 1px solid black; text-align: center;">0</td> <td style="text-align: center;">0</td> <td style="text-align: center;">0</td> <td style="border-right: 1px solid black; text-align: center;">0</td> <td style="text-align: center;">0</td> <td style="padding: 5px;">← System disarmed → no points tripped</td> </tr> <tr> <td style="border-right: 1px solid black; 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text-align: center;">0</td> <td style="text-align: center;">1</td> <td rowspan="4" style="padding: 5px;">} System disarmed → glass broken so alarm should sound</td> </tr> <tr> <td style="border-right: 1px solid black; text-align: center;">0</td> <td style="text-align: center;">1</td> <td style="text-align: center;">0</td> <td style="border-right: 1px solid black; text-align: center;">1</td> <td style="text-align: center;">1</td> </tr> <tr> <td style="border-right: 1px solid black; text-align: center;">0</td> <td style="text-align: center;">1</td> <td style="text-align: center;">1</td> <td style="border-right: 1px solid black; text-align: center;">0</td> <td style="text-align: center;">1</td> </tr> <tr> <td style="border-right: 1px solid black; text-align: center;">0</td> <td style="text-align: center;">1</td> <td style="text-align: center;">1</td> <td style="border-right: 1px solid black; text-align: center;">1</td> <td style="text-align: center;">1</td> </tr> <tr> <td style="border-right: 1px solid black; 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Solution: $X = G + A \cdot D + A \cdot M$